Response from the London Mathematical Society

Our comments relate to Statistics (at GCSE and at A/AS level)

The consultation process. Before presenting our response in 1-3 below we would like to express our concern at the procedures adopted in the reform of these qualifications. As with other recent reforms, the procedure makes plain the lack (which we and others have often pointed out) of a body which oversees curriculum reform and development, ensuring proper, effective and transparent use of expertise as well as coherence and intellectual rigour.

Particular concerns include:

- The consultations on content and assessment are being made simultaneously. Normal procedure is first to agree content, and then to design an appropriate assessment.

- It is not clear who has drawn up the documents setting out the proposed content for these qualifications. One can merely infer something about this in the information about from Annex 1 of the DfE subject content consultation document where it lists those who were consulted (rather than those who were the primary writers).

- According to the consultation document ‘Awarding organisations were unable to consult with all subject groups and we welcome the input of organisations, teachers and students in this public consultation’. This suggests that awarding organisations have drawn up the content. If this is correct, then a serious departure from proper procedure seems to have occurred. Policy for curriculum content is not supposed to be determined by these bodies, although of course they may be consulted.

- Consultation is at a late stage in proceedings (we have been told policy will be published two weeks after the closing date of the consultation). This is particularly serious given the admitted gaps in the consultation process at earlier stages.

- Apart from reference to GCSE Mathematics, which may be taken simultaneously with GCSE statistics, there is little sign that full account has been taken of current developments of the assessment of statistics in Mathematics qualifications including particularly Mathematics A-level (which will have a compulsory statistics element) or the new Core Maths qualifications (of which there is no mention).

1. A/AS level Statistics. We see no possible justification for including a specification for “Statistics AS/A level” within the current review.

1.1 The government’s own “productivity plan” (July 2015) states clearly that:
   “the government will simplify and streamline the number of qualifications so that individuals have a clear set of routes which allow for progression to high level skills, rather than thousands of qualifications.” (p. 25)
1.2 Statistics is now a compulsory part of all A/AS level “Mathematics” courses, which are currently taken by more than 160 000 students each year.

Statistics is also a major constituent of all “Core mathematics” syllabuses, which are being developed as the preferred numerate qualification for those who choose not to study mathematics at A/AS level.

1.3 Hence, the only conceivable reason for including a specification for “A/AS level Statistics” would be if there were a significant additional cohort of potential candidates, whose needs would not be addressed by the provision outlined in 1.2. Current A/AS level provision suggests the precise opposite.

[Evidence supporting this claim: As far as we can tell, there is currently just one A level in Statistics, which attracted 811 entries in 2015; and two AS levels – one attracting 1601 entries and the other attracting just 29 entries in 2015. Hence bland references in the consultation document to what AS and A levels in Statistics “build upon” (para 2), “encourage” (para 3), “assume” (para 4), “require” (paras 5-8), etc. – which give the impression that we are discussing well-established qualifications, which has to be replicated in any new regime, are thoroughly misleading.]

1.4 In these circumstances, if the government commitment to “simplifying the number of qualifications so that individuals have a clear set of progression routes” means anything at all, then it would seem to imply that the A/AS level Statistics specification should be discontinued.

1.5 Statistics is widely used within many A-level subjects. We would also like to draw attention to recent report by ACME and The Royal Statistical Society on Embedding Statistics at A-level. This report does not seem to identify a role for A-level Statistics, or even mention it.

2. GCSE Statistics: Background. In contrast, there would seem to be positive reasons for retaining a GCSE Statistics qualification. However, the details relating to (a) the content specification and (b) its assessment need to be competently and openly drafted, widely scrutinised, and transparently adapted in the light of comments received. It is hard to see how this can be achieved under the present arrangement whereby the two interacting functions are handled separately – yet simultaneously – with a very short period allowed for comments to be assessed and acted upon.

The current draft, and the manner in which the work has been handled up to this point, should be unacceptable in an open society. The published timeline for first assessment may incline officials to “soldier on” regardless; but to do so would be wrong. Even though “GCSE Statistics” is a relatively minor qualification, the shortcomings in the drafting, and the apparent lack of discussion in the relevant community must be addressed as a matter of urgency.

2.1 The changed rules relating to GCSE results (where only the first result obtained contributes to certain school accountability measures) appear to have reduced the number of ‘early entry’ candidates (those taking GCSE Mathematics entries before the summer of Year 11). This is to be welcomed.

This trend has consequences for GCSE Statistics. In the past, those who achieved a reasonable GCSE Mathematics grade by the end of Year 10 were often “rewarded” by being entered for GCSE
Statistics in Year 11. This was entirely inappropriate – but the practice seems to have diminished to some extent in recent years. (Between 2013 and 2015, early entries for GCSE Mathematics dropped by over 100,000, and the number of entries in Year 11 rose by over 100,000. In the same period, entries for GCSE Statistics in Year 10 or below almost doubled to 29,212, while entries in Year 11 fell from a high of 34,730 in 2014 to 26,597 in 2015. So it looks as though students are increasingly being entered for GCSE Statistics before taking GCSE Mathematics – rather than the other way round.)

Note: This makes the GCSE Statistics entry larger than that for German or Music, and roughly half the size of Physics, or Chemistry or Biology or ICT.

We therefore see considerable potential value in having a GCSE Statistics available for a range of abilities, provided central pressure continues to ensure that it is not the main numerate subject studied in Year 11.

2.2 However, there are two features of the design implicit in the draft, which need to be changed.

2.3 The simplest change that is needed concerns coursework. Whether candidates are taking GCSE Statistics because they find mathematics easy, or to provide practical support for their numerate development, there is no escaping from the extent to which learning statistics, and assessing that learning, demands a strong practical element.

2.3.1 The requirement seems so clear, that the lack of such an emphasis in both the draft content and in the assessment can only be explained in terms of an understandable, but over-zealous, bureaucratic commitment to assessing solely through exams wherever possible.

2.3.2 In the case of GCSE Statistics, both the discipline itself and the educational value which it can offer to students, would seem to demand a specification which presumes, and an assessment regime which incorporates, a suitable coursework component.

2.3.3 In core subjects, we understand the administrative reasons for wanting to control the coursework component of assessment wherever possible. But GCSE Statistics lies outside the EBacc; so there is no reason why its educational and assessment character should be approached more dogmatically than other academic, vocational, and arts qualifications that ‘supplement’ the EBacc subjects within “Progress 8” or “Attainment 8”. We suspect that a coursework, or practical, component is fairly common in other qualifications which ‘supplement’ the EBacc core; so it is hard to see why anyone should try to distort GCSE Statistics by denying it the same opportunity.

2.4 The more serious change that is needed is to urgently subject the draft specification to the scrutiny of an experienced panel of curriculum drafters

(a) to eliminate some of its more undesirable features, and

(b) to consider carefully any essential, but more substantial, changes.

If the draft were the result of a transparent process, one might list a small number of improvements. To do so here would convey the wrong impression – even though some bits made no sense to us (so it is hard to assess the impression of ‘overload’; or the misguided bias in favour of ‘advanced’ methods which will not be understood, at the expense of expecting a robust understanding of basic statistics). What is needed is a thorough and open review.
2.5: The overlap between this specification and that for GCSE Mathematics certainly needs careful thought: some material should definitely appear in both syllabuses, but needs to be given a clearly distinctive flavour in the Statistics syllabus.

Further thought is also needed concerning:

(i) the exclusion of some material which would seem to be important (such as the idea of a “null hypothesis”), and
(ii) the confusion of key ideas which deserve to be more clearly stated (such as the fact that the highlighted summary in “A” (para 8 on page 4) should begin by emphasising the kind of questions, or hypotheses that can be subjected to statistical scrutiny, and that a statistical enquiry needs to identify such a question, or hypothesis, before moving on to consider what data to collect, or how to collect it)
(iii) the inclusion of some material, which appears arbitrary, or which is not liable to quantitative analysis at GCSE level, or which cannot really be understood at this level (thereby officially encouraging a “cook-book” approach – which is especially worrying when fundamental ideas are presented in the content draft as things candidates merely need to “know” – with no recognition or indication of their subtlety: see e.g. section E).

The flaw indicated in (iii) pervades the whole specification, where one finds an emphasis on words at the expense of key ideas: (e.g. Is the idea of a distribution addressed appropriately anywhere? If so, we missed it.) We realise that part of the challenge of GCSE Statistics is to raise questions that are far more subtle than mere “applied number”; but the draft fails to clarify how the emphasis on language and ideas in pages 3-6 relates to the techniques implicit in pages 6-8.

More worrying still is the blatant attempt to re-frame the whole of statistics teaching in England in terms of “the statistical enquiry cycle” via Appendix 4 of a draft content list, which has never been openly debated, or refined. This is simply wrong.

The idea of a “statistical enquiry cycle” can be helpful; but the version concocted in Appendix 4 of the content draft does not appear to have been trialled or refined in any way. The idea has some strengths: e.g. it recognises the need to start with a question or hypothesis. But the proposed form also has major shortcomings: e.g. the “cycle” is never summarised in memorable form – as, for example, in Porkess’s four-stage cycle, or in New Zealand’s five stage PPDAC [Problem, Plan, Data, Analysis, Conclusion], and the proposed version has a disproportionate emphasis on qualitative presentation at the expense of analysis.)

It may be that content and assessment can usefully be framed in such terms – but in the absence of open discussion, professional consensus, trialling, and consequent refinement, nothing is gained (and much may be lost) by replacing familiar criteria by an unfamiliar, opaque, mantra “the statistical enquiry cycle” – especially one which is so elaborated so poorly (in Appendix 4).


Ad 3.78 (in the consultation): It is not possible to draft viable assessment principles on the basis of a “review of the proposed subject content”, when that subject content has been subjected to no
evident scrutiny, and no-one seems to know how it was drafted, by whom, or in response to what brief.

We can envisage no defensible list of content for GCSE Statistics which would warrant the bald assertion that “all of the content can be assessed through exams”. Nor do we see any reason why this should be the preferred conclusion for a non-EBacc subject such as GCSE Statistics.

Ad 3.79: It is not clear where the “principles” to which you appeal are listed, or what they are based upon. We have sympathy with the goals (validity, etc.). But in this case, any possible loss in interpreting your guiding “principle” would be far outweighed by the educational gain from including a practical, or coursework, element in the assessment.

Ad 3.80-3.85: Those with experience of teaching existing GCSE Statistics courses find it hard to see how one could eliminate tiering. (If we are ever to move towards untiered assessment, then before any national change is proposed it is essential first to engage in trials and piloting in order to check that we know how to design and teach using untiered papers.)

Ad 3.86: Viable “Assessment Objectives” inevitably depend to some extent on the intended content. And given the unsatisfactory state of the proposed content list, and the remarkable (unprecedented?) attempt to “consult” on both content and assessment simultaneously, it is hard for outsiders to make comments that might help to improve the final version. However, we shall try.

- The proposed AOs do not “specify more clearly” (as claimed in 3.86).
  - In particular
    - the proposed AO1 is adequately covered by the old AO1, AO2, AO3; the proposed AO2 is covered by the old AO3; the proposed AO3 is covered by the old AO3. AO4; the proposed AO4 is covered by the old AO4
    - simple words, and a familiar framework, have been replaced by fancy language, whose meaning is often left opaque:
      [AO1: “methodologies” ?; which “notation” is “necessary”?;
      AO2: this should include “recording” (“for the collection, recording and visualisation of data”)
      AO1, AO3, AO4: The idea of a “statistical enquiry cycle” can be helpful; but the version concocted in Appendix 4 of the content draft does not appear to have been trialled or refined in any way. The idea has some strengths: e.g. it recognises the need to start with a question or hypothesis – an idea which is insufficiently clarified elsewhere. But the proposed form also has major shortcomings: e.g. the “cycle” is never summarised in memorable form – as, for example, in Porkess’s four-stage cycle, or in New Zealand’s five stage PPDAC [Problem, Plan, Data, Analysis, Conclusion]. The proposed version also has a disproportionate emphasis on qualitative presentation at the expense of analysis.]
      It may be that content and assessment can usefully be framed in such terms – but in the absence of open discussion, professional consensus, trialling, and consequent refinement, nothing is gained (and much may be lost) by replacing familiar criteria by an unfamiliar, opaque, mantra “the statistical enquiry cycle”.
      Etc.]
It may be possible in theory to devise a completely different set of AOs; but the improvement should justify the discontinuity of such a major change (which makes it harder for teachers to interpret what is intended).

Hence it is unclear how persons unknown were allowed to use the current review to introduce such a radical change – whereby everything becomes dependent on an idiosyncratic, poorly explained, and apparently untested/unrefined “statistical enquiry cycle” – without prior professional debate.

**We therefore urge you to replace the proposed AOs by an improved version of the current AOs (by mild ‘tweaking’):** for example

- the old AO1 seems fine as it stands
- the old AO2 might be improved by inserting “organise, and record” at the end to read: “Describe and use appropriate methods to select, collect, organise, and record data”
- the old AO3 seems fine
- the old AO4 might be improved by inserting the words “and techniques” to read: “Use statistical evidence and techniques to identify inferences, make deductions and draw conclusions”

The allocated weightings should probably depend on the tier being considered (as with the GCSE Mathematics weightings.

**Question 75:** To what extent do you agree or disagree that GCSEs in statistics should be assessed entirely by exams?

*We disagree strongly.*

**Question 76:** To what extent do you agree or disagree that GCSEs in statistics should be tiered?

*In the absence of evidence to the contrary, we agree.*

**Question 77:** To what extent do you agree or disagree that we should adopt a similar approach to tiering in GCSE statistics as we have for GCSE mathematics?

*In the absence of evidence to the contrary, we agree.*

**Question 78:** To what extent do you agree or disagree that the proposed assessment objectives are appropriate for GCSEs in statistics?

*The proposed AOs are unfamiliar, untried, hence inappropriate (perhaps unworkable). We advise you to back up, and improve the current AOs by ‘tweaking’ (see Q 79).*

**Question 79:** To what extent do you agree or disagree that the proposed weightings of the assessment objectives are appropriate for GCSEs in statistics?

*We reject the proposed AOs. Please use the experience of existing Awarding Bodies to ‘tweak’ the current weightings – perhaps allowing Foundation and Higher tier to have different weightings.*

**Question 80:** Do you have any further comments relating to the assessment of this subject?

*See above. (In particular, we plead for an urgent review of the draft content, and of the doctrinaire exclusion of a practical or coursework element).*